

1E3101

Roll No.

Total No. of Pages: **4****1E3101****B. Tech. I - Sem. (Main / Back) Exam., - 2025
1FY2-01 Engineering Mathematics - I****Time: 3 Hours****Maximum Marks: 70***Instructions to Candidates:**Attempt all ten questions from Part A, five questions out of seven questions from Part B and three questions out of five from Part C.**Schematic diagrams must be shown wherever necessary. Any data you feel missing may suitably be assumed and stated clearly. Units of quantities used /calculated must be stated clearly.**Use of following supporting material is permitted during examination.
(Mentioned in form No. 205)*1. NIL2. NIL**PART – A****[10×2=20]****(Answer should be given up to 25 words only)****All questions are compulsory**Q.1 Evaluate - $\int_0^1 x^2(1-x)^3 dx$ Q.2 Test the convergence of $\int_1^{\infty} \frac{dx}{x^{3/2}}$.

Q.3 What is Convergence and Divergence of a sequence?

Q.4 Find the interval of convergence of Exponential and Logarithmic series.

Q.5 Write Euler's formula of Fourier Series.

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- Q.6 Find half range sine series for the function $f(x) = x$ in the interval $0 < x < z$.
- Q.7 If $u = e^{xyz}$, then find $\frac{\partial^3 u}{\partial x \partial y \partial z}$.
- Q.8 Write the equation of the tangent plane to the surface $z = f(x, y)$.
- Q.9 Change the order of integration and then evaluate - $\int_0^1 \int_{x^2}^{2-x} xy \, dx \, dy$.
- Q.10 Write the statement of Green theorem.

PART – B

[5×4=20]

(Analytical/Problem solving questions)

Attempt any five questions

- Q.1 Show that $\int_0^\infty \frac{x^2 \, dx}{(1+x^4)^3} = \frac{5\pi\sqrt{2}}{128}$. <https://www.rtuonline.com>
- Q.2 Test for convergence of the series $\sum \frac{1}{\sqrt{n} + \sqrt{n+1}}$.
- Q.3 Find the Fourier series to represent $f(x) = |x|$ for $-\pi < x < \pi$.
- Q.4 Find the directional derivative of $\phi = x^2 - 2y^2 + 4z^2$ at $(1, 1, -1)$ in the direction of the vector $2\hat{i} + \hat{j} - \hat{k}$. Also find the direction of maximum directional derivative at $(1, 1, -1)$ and its max value.
- Q.5 Find the limit and test for continuity of the function
- $$f(x, y) = \begin{cases} \frac{x^3 - y^3}{x + y} & \text{if } x + y \neq 0 \\ 0 & \text{if } x + y = 0 \end{cases} \text{ at the point } (0, 0).$$
- Q.6 Evaluate $\iint_R (x^2 + y^2) \, dx \, dy$ where R is the region bounded by $y = x$ and $y^2 = 4x$.
- Q.7 Evaluate $\iiint_V f \, dV$ where $f = 2x + y$, V is the closed region bounded by the cylinder $z = 4 - x^2$ and the plane $x = y = z = 0$ and $y = z$.

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PART – C

[3×10=30]

(Descriptive/Analytical/Problem Solving/Design Questions)

Attempt any three questions

- Q.1 Find the Fourier Series to represent $f(x) = x - x^2$ in the interval $-1 < x < 1$.
- Q.2 Test the convergence of the series $\frac{1^2}{2^2} + \frac{1^2 \cdot 3^2}{2^2 \cdot 4^2} + \frac{1^2 \cdot 3^2 \cdot 5^2}{2^2 \cdot 4^2 \cdot 6^2} + \dots$
- Q.3 If $u = f(r)$, $r^2 = x^2 + y^2$ show that $\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} = f''(r) + \frac{1}{r} f'(r)$.
- Q.4 Find the volume of greatest rectangular parallelepiped inscribed in the ellipsoid whose equation is $\frac{x^2}{a^2} + \frac{y^2}{b^2} + \frac{z^2}{c^2} = 1$.
- Q.5 Verify Stokes theorem for $F = (x^2 + y - 4)\hat{i} + 3xy\hat{j} + (2xz + z^2)\hat{k}$ over the surface of the hemisphere $x^2 + y^2 + z^2 = 16$ above the xy plane.
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